

Electric Potential (II)

Text sections 25.3, 25.5

- Potential of a point charge
- Potential of several point charges
- Potential energy of a collection of charges

Practice: Chapter 25,
Objective Questions 5, 7, 9, 10
Problems 18, 21, 27, 35

Review: Electric Potential

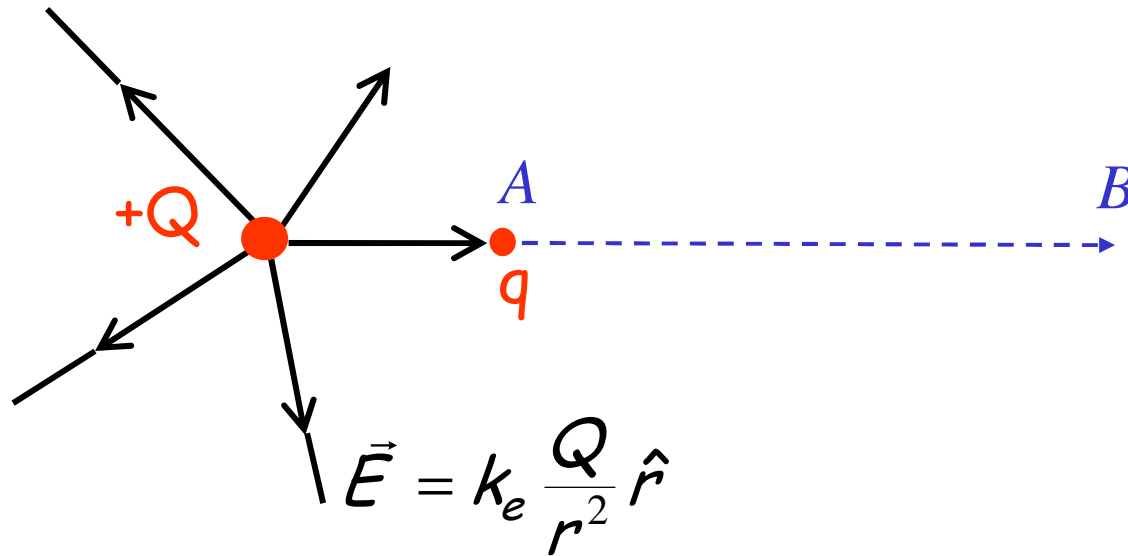
$$V \equiv \frac{\text{potential energy}}{\text{charge}}$$

So, $dW = -qdV = q\mathbf{E} \cdot d\mathbf{s}$

$$-dV = \mathbf{E} \cdot d\mathbf{s}$$

$$E_x = -\frac{dV}{dx}$$

What is the electric potential near a point charge Q ?



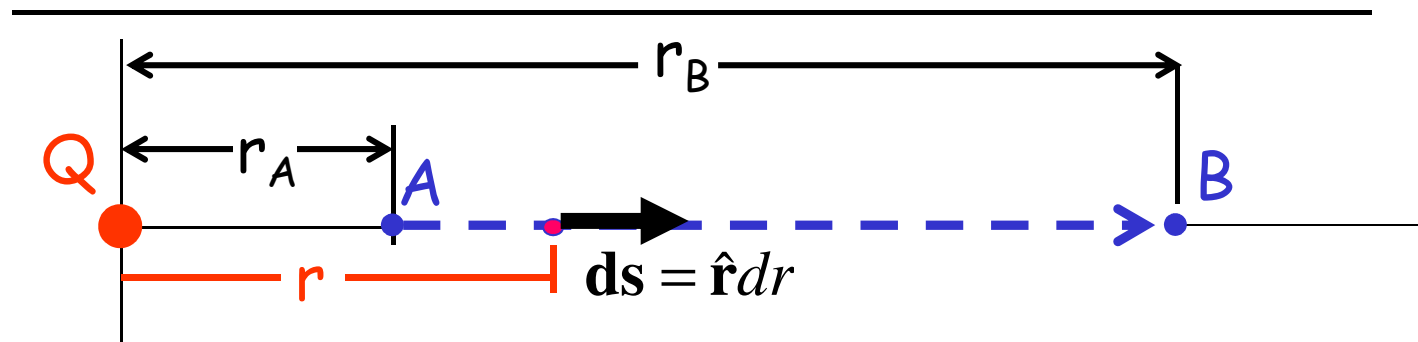
Move *another* charge q in the field:
its **potential energy** changes as the field does work.

$$q(V_B - V_A) = -(\text{work}) = -\int_{r_A}^{r_B} (q\mathbf{E}) \cdot d\mathbf{s}$$

... then cancel q on each side.

Details: Move from A to B along a radial line,

$$-dV = \mathbf{E} \cdot d\mathbf{s} = E dr = k_e \frac{Q}{r^2} dr$$



$$\int_A^B dV = - \int_{r_A}^{r_B} \frac{k_e Q}{r^2} dr$$
$$\Rightarrow V_B - V_A = +k_e Q \left[\frac{1}{r_B} - \frac{1}{r_A} \right]$$

Set $V=0$ as $r \rightarrow \infty$

Then...

$$V = \frac{k_e Q}{r}$$

(potential around a single point charge Q)

What shape are the equipotential surfaces near a single point charge?

What is the potential 10 cm from a (point) charge of 100 nC ?

How will the result change for a spherical charge (which is not a "point charge")?

QUIZ

What shape are the equipotential surfaces near a single positive point charge?

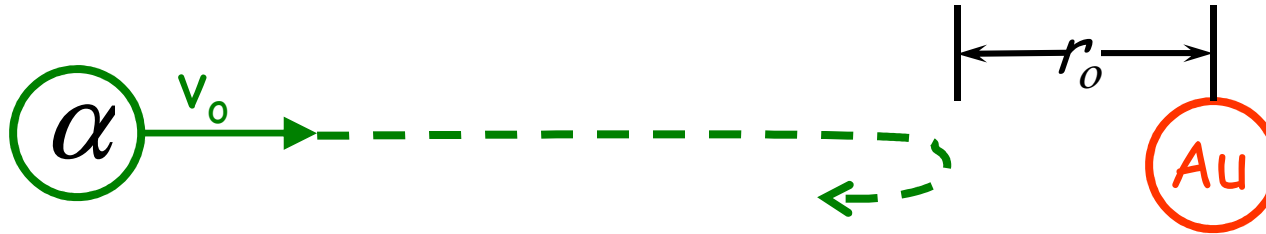
- A) radial lines outwards
- B) radial lines inwards
- C) concentric spheres
- D) vertical planes
- E) horizontal planes

Equipotentials



Example: Rutherford Experiment

How close can a fast charged particle get to a gold nucleus?



Alpha particle:

$$m_{\alpha} = 6.67 \times 10^{-27} \text{ kg}$$

$$q = +2e$$

$$v_0 = 1.0 \times 10^7 \text{ m/s}$$

Gold nucleus:

$$Q = +79e$$

(stationary)

Find: a) Initial K.E. of α in electron-volts. (answer: 2.08 MeV)

b) P.E. of α at $r = r_0$

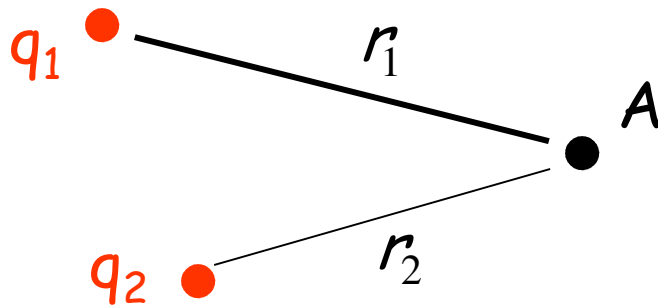
c) V at $r = r_0$

d) r_0

(answer: $1.13 \times 10^{-13} \text{ m}$)

Potential of Several Point Charges

- Potentials add (as *scalars!*)



At A: $V = k\left(\frac{q_1}{r_1} + \frac{q_2}{r_2}\right)$

In General:

$$V = \sum_i k_e \frac{q_i}{r_i}$$

Or...

$$V = \int k_e \frac{dq}{r}$$

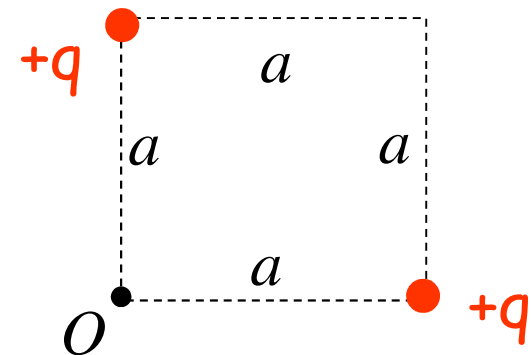
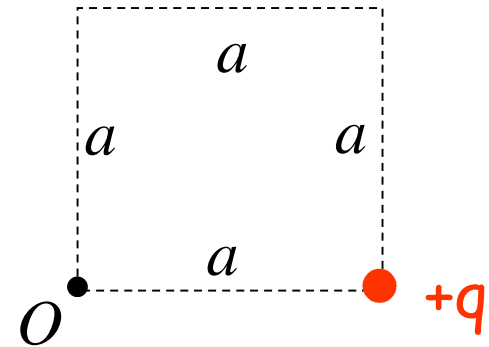
← (continuous charge distribution)

Quiz:

A single charge q produces a potential $V_0 = 1000 \text{ V}$ at point O .

What is the potential at point O due to the two identical charges?

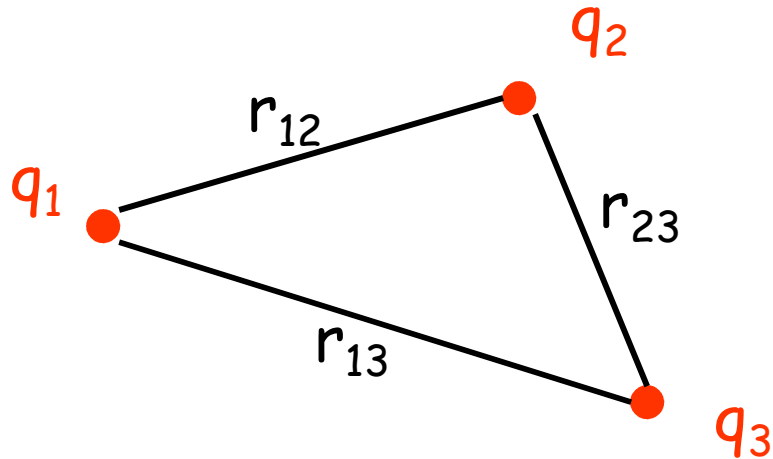
- A) 1000 V
- B) 1414 V
- C) 2000 V
- D) 2828 V



Electrostatic Potential Energy

What is the total potential energy of 3 (or more) point charges?

(Fine Print: assume $U = 0$ when all point charges are at infinity)



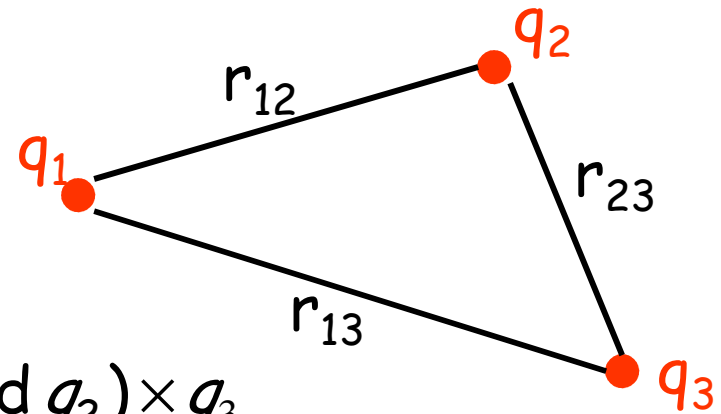
$$U = \sum_{\text{pairs } ij} k \frac{q_i q_j}{r_{ij}}$$

Derivation: Bring 3 charges in from infinity...

First Charge: no work needed (q_1)

Second Charge: $U_{12} = (V \text{ of } q_1) \times q_2$

$$= k \frac{q_1 q_2}{r_{12}}$$



Third Charge: Work needed

$$= (\text{potential of } q_1 \text{ and } q_2) \times q_3$$

$$= k \left(\frac{q_1}{r_{13}} + \frac{q_2}{r_{23}} \right) q_3$$

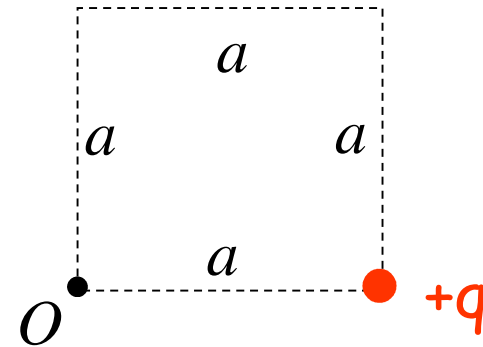
Total =

$$U_{total} = k \left(\frac{q_1 q_2}{r_{12}} + \frac{q_1 q_3}{r_{13}} + \frac{q_2 q_3}{r_{23}} \right)$$

$$U = \sum_{\text{pairs } ij} k \frac{q_i q_j}{r_{ij}}$$

Quiz:

A single charge $q=1.0\mu\text{C}$ produces a potential $V_0 = 1000\text{ V}$ at point O .



What is the total potential energy of the four identical charges?

- A) 4.0 mJ
- B) 3.0 mJ
- C) 6.0 mJ
- D) none of the above

